A Activities for Learning, Inc.

RIGHTSTARTTM MATHEMATICS

by Joan A. Cotter, Ph.D.

LEVEL B LESSONS

FOR HOME EDUCATORS



Special thanks to Sharalyn Colvin, who converted *RightStart™ Mathematics: Grade 1 Lessons* into *RightStart™ Mathematics: Level B For Home Educators.*

Note: Rather than use the designation, K-4, to indicate a grade, levels are used. Level A is kindergarten, Level B is first grade, and so forth.

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RIghtStart™ MATHEMATICS: OBJECTIVES FOR LEVEL B

Name	Year _			
Teacher				
Numeration	1ST QTR	2ND QTR	3RD QTR	4TH QTR
Can recognize quantities 1 to 5 and represent it on abacus				
Knows even numbers to 20				
Knows odd numbers to 19				
Can identify even/odd numbers to 100				
Can count by 2s to 30	N/A			
Can count by 5s to 50	N/A			
Can count by 10s to 100	N/A			
Money	ļ -			
Knows name and value of penny, nickel, dime, and quarter				
Can determine the value of three coins				
Place Value				
Can trade 10 ones for 1 ten				
Can trade 10 tens for 1 hundred				
Can trade 10 hundreds for 1 thousand				
Knows 37 as 3-ten 7				
Can read four-place numbers				
Knows traditional names: e.g., 18 as eighteen as well as 1-ten 8	N/A			
Addition	ļ .			
Understands addition as combining parts to form whole				
Can add 4-digit numbers	N/A	N/A	N/A	
Knows number facts equal to 10				
Knows number facts up to 18	N/A	N/A	N/A	
Can add 2-digit numbers mentally	N/A	N/A		
Subtraction			•	
Understands subtraction as missing addend	N/A			
Understands subtraction as separating	N/A			
Knows number facts subtracting from numbers up to 10	N/A			
Calculator				
Can add and subtract whole numbers	N/A	N/A	N/A	
Problem Solving	,			
Can solve change problems				
Can solve combine problems	N/A			
Can solve equalize problems	N/A	N/A	N/A	
Geometry	<u>'</u>			
Knows square is a special rectangle				
Knows parallel and perpendicular lines	N/A			
Knows what a reflection is	N/A			
Time	<u> </u>			
Knows days of the week and months of the year	N/A			
Can tell time to five-minute intervals	N/A	N/A		
Can tell time to the minute	N/A	N/A		
Measurement	1			
Can determine length with nonstandard measure	N/A	N/A	N/A	
Can find perimeter	N/A	N/A	N/A	
Can read scales with numbers missing	N/A	N/A	N/A	
Fractions	-			
Can divide into halves and fourths	N/A	N/A	N/A	
Knows unit fractions up to 1/10				

How This Program Was Developed

We have been hearing for years that Japanese students do better than U.S. students in math in Japan. The Asian students are ahead by the middle of first grade. And the gap widens every year thereafter.

Many explanations have been given, including less diversity and a longer school year. Japanese students attend school 240 days a year.

A third explanation given is that the Asian public values and supports education more than we do. A first grade teacher has the same status as a university professor. If a student falls behind, the family, not the school, helps the child or hires a tutor. Students often attend after-school classes.

A fourth explanation involves the philosophy of learning. Asians and Europeans believe anyone can learn mathematics or even play the violin. It is not a matter of talent, but of good teaching and hard work.

Although these explanations are valid, I decided to take a careful look at how mathematics is taught in Japanese first grades. Japan has a national curriculum, so there is little variation among teachers.

I found some important differences. One of these is the way the Asians name their numbers. In English we count ten, eleven, twelve, thirteen, and so on, which doesn't give the child a clue about tens and ones. But in Asian languages, one counts by saying ten-1, ten-2, ten-3 for the teens, and 2-ten 1, 2-ten 2, and 2-ten 3 for the twenties.

Still another difference is their criteria for manipulatives. Americans think the more the better. Asians prefer very few, but insist that they be imaginable, that is, visualizable. That is one reason they do not use colored rods. You can imagine the one and the three, but try imagining a brown eight—the quantity eight, not the color. It cannot be done without grouping.

Another important difference is the emphasis on non-counting strategies for computation. Japanese children are discouraged from counting; rather they are taught to see quantities in groups of fives and tens.

For example, when an American child wants to know 9+4, most likely the child will start with 9 and count up 4. In contrast, the Asian child will think that if he takes 1 from the 4 and puts it with the 9, then he will have 10 and 3, or 13. Unfortunately, very few American first-graders at the end of the year even know that 10+3 is 13.

I decided to conduct research using some of these ideas in two similar first grade classrooms. The control group studied math in the traditional workbook-based manner. The other class used the lesson plans I developed. The children used that special number naming for three months.

They also used a special abacus I designed, based on fives and tens. I asked 5-year-old Stan how much is 11 + 6. Then I asked him how he knew. He replied, "I have the abacus in my mind."

The children were working with thousands by the sixth week. They figured out how to add 4-digit numbers on paper after learning how on the abacus.

Every child in the experimental class, including those enrolled in special education classes, could add numbers like 9 + 4, by changing it to 10 + 3.

I asked the children to explain what the 6 and 2 mean in the number 26. Ninety-three percent of the children in the experimental group explained it correctly while only 50% of third graders did so in another study.

I gave the children some base ten rods (none of them had seen them before) that looked like ones and tens and asked them to make 48. Then I asked them to subtract 14. The children in the control group counted 14 ones, while the experimental class removed 1 ten and 4 ones. This indicated that they saw 14 as 1 ten and 4 ones and not as 14 ones. This view of numbers is vital to understanding algorithms, or procedures, for doing arithmetic.

I asked the experimental class to mentally add 64 + 20, which only 52% of nine-year-olds on the 1986 National test did correctly; 56% of those in the experimental class could do it.

Since children often confuse columns when taught traditionally, I wrote 2304 + 86 = horizontally and asked them to find the sum any way they liked. Fifty-six percent did so correctly, including one child who did it in his head.

The following year I revised the lesson plans and both first grade classes used these methods. I am delighted to report that on a national standardized test, both classes scored at the 98th percentile.

Joan A. Cotter, Ph.D.

Some General Thoughts on Teaching Mathematics

- 1. Only five percent of mathematics should be learned by rote; 95 percent should be understood.
- 2. Real learning builds on what the child already knows. Rote teaching ignores it.
- 3. Contrary to the common myth, "young children can think both concretely and abstractly. Development is not a kind of inevitable unfolding in which one simply waits until a child is cognitively 'ready." —Foundations for Success NMAP
- 4. What is developmentally appropriate is not a simple function of age or grade, but rather is largely contingent on prior opportunities to learn." —Duschl & others
- 5. Understanding a new model is easier if you have made one yourself. So, a child needs to construct a graph before attempting to read a ready-made graph.
- 6. Good manipulatives cause confusion at first. If a new manipulative makes perfect sense at first sight, it is not needed. Trying to understand and relate it to previous knowledge is what leads to greater learning. —Richard Behr & others.
- 7. According to Arthur Baroody, "Teaching mathematics is essentially a process of translating mathematics into a form children can comprehend, providing experiences that enable children to discover relationships and construct meanings, and creating opportunities to develop and exercise mathematical reasoning."
- 8. Lauren Resnick says, "Good mathematics learners expect to be able to make sense out of rules they are taught, and they apply some energy and time to the task of making sense. By contrast, those less adept in mathematics try to memorize and apply the rules that are taught, but do not attempt to relate these rules to what they know about mathematics at a more intuitive level."
- 9. Mindy Holte puts learning the facts in proper perspective when she says, "In our concern about the memorization of math facts or solving problems, we must not forget that the root of mathematical study is the creation of mental pictures in the imagination and manipulating those images and relationships using the power of reason and logic." She also emphasizes the ability to imagine or visualize, an important skill in mathematics and other areas.
- 10. The only students who like flash cards are those who do not need them.
- 11. Mathematics is not a solitary pursuit. According to Richard Skemp, solitary math on paper is like reading music, rather than listening to it: "Mathematics, like music, needs to be expressed in physical actions and human interactions before its symbols can evoke the silent patterns of mathematical ideas (like musical notes), simultaneous relationships (like harmonies) and expositions or proofs (like melodies)."
- 12. "More than most other school subjects, mathematics offers special opportunities for children to learn the power of thought as distinct from the power of authority. This is a very important lesson to learn, an essential step in the emergence of independent thinking." —*Everybody Counts*

- 13. The role of the teacher is to encourage thinking by asking questions, not giving answers. Once you give an answer, thinking usually stops.
- 14. Putting thoughts into words helps the learning process.
- 15. Help the children realize that it is their responsibility to ask questions when they do not understand. Do not settle for "I don't get it."
- 16. The difference between a novice and an expert is that an expert catches errors much more quickly. A violinist adjusts pitch so quickly that the audience does not hear it.
- 17. Europeans and Asians believe learning occurs not because of ability, but primarily because of effort. In the ability model of learning, errors are a sign of failure. In the effort model, errors are natural. In Japanese classrooms, the teachers discuss errors with the whole class.
- 18. For teaching vocabulary, be sure either the word or the concept is known. For example, if a child is familiar with six-sided figures, we can give him the word, hexagon. Or, if he has heard the word, multiply, we can tell him what it means. It is difficult to learn a new concept and the term simultaneously.
- 19. Introduce new concepts globally before details. This lets the children know where they are headed.
- 20. Informal mathematics should precede paper and pencil work. Long before a child learns how to add fractions with unlike denominators, she should be able to add one half and one fourth mentally.
- 21. Some pairs of concepts are easier to remember if one of them is thought of as dominant. Then the non-dominant concept is simply the other one. For example, if even is dominant over odd; an odd number is one that is not even.
- 22. Worksheets should also make the child think. Therefore, they should not be a large collection of similar exercises, but should present a variety. In RightStart™ Mathematics, they are designed to be done independently.
- 23. Keep math time enjoyable. We store our emotional state along with what we have learned. A person who dislikes math will avoid it and a child under stress stops learning. If a lesson is too hard, stop and play a game. Try the lesson again later.
- 24. In Japan students spend more time on fewer problems. Teachers do not concern themselves with attention spans as is done in the U.S.
- 25. In Japan the goal of the math lesson is that the student has understood a concept, not necessarily has done something (a worksheet).
- 26. The calendar must show the entire month, so the children can plan ahead. The days passed can be crossed out or the current day circled.
- 27. A real mathematical problem is one in which the procedures to find the answer is not obvious. It is like a puzzle, needing trial and error. Emphasize the satisfaction of solving problems and like puzzles, of not giving away the solution to others.

RightStart™ Mathematics

Ten major characteristics make this research-based program effective:

- 1. Refers to quantities of up to 5 as a group; discourages counting individually. Uses fingers and tally sticks to show quantities up to 10; teaches quantities 6 to 10 as 5 plus a quantity, for example 6 = 5 + 1.
- 2. Avoids counting procedures for finding sums and remainders. Teaches five- and ten-based strategies for the facts that are both visual and visualizable.
- 3. Employs games, not flash cards, for practice.
- 4. Once quantities 1 to 10 are known, proceeds to 10 as a unit. Temporarily uses the "math way" of naming numbers; for example, "1 ten-1" (or "ten-1") for eleven, "1-ten 2" for twelve, "2-ten" for twenty, and "2-ten 5" for twenty-five.
- 5. Uses expanded notation (overlapping) place-value cards for recording tens and ones; the ones card is placed on the zero of the tens card. Encourages a child to read numbers starting at the left and not backward by starting at the ones.
- 6. Proceeds rapidly to hundreds and thousands using manipulatives and placevalue cards. Provides opportunities for trading between ones and tens, tens and hundreds, and hundreds and thousands with manipulatives.
- 7. Teaches mental computation. Investigates informal solutions, often through story problems, before learning procedures.
- 8. Teaches four-digit addition on the abacus, letting the child discover the paper and pencil algorithm.
- 9. Introduces fractions with a linear visual model, including all fractions from 1/2 to 1/10. "Pies" are not used initially because they cannot show fractions greater than 1. Later, the tenths will become the basis for decimals.
- 10. Teaches short division (where only the answer is written down) for single-digit divisors, before long division.

Second Edition

Many changes have occurred since the first RightStart™ lessons were begun in 1994. First, mathematics is used more widely in many fields, for example, architecture, science, technology, and medicine. Today, many careers require math beyond basic arithmetic. Second, research has given us new insights into how children learn mathematics. Third, kindergarten has become much more academic, and fourth, most children are tested to ensure their preparedness for the next step.

This second edition is updated to reflect new research and applications. Topics within a grade level are always taught with the most appropriate method using the best approach with the child and teacher in mind.

Daily Lessons

Objectives. The objectives outline the purpose and goal of the lesson. Some possibilities are to introduce, to build, to learn a term, to practice, or to review.

Materials. The Math Set of manipulatives includes the specially crafted items needed to teach RightStart™ Mathematics. Occasionally, common objects such as scissors will be needed. These items are indicated by boldface type.

Warm-up. The warm-up time is the time for quick review, memory work, and sometimes an introduction to the day's topics. The dry erase board makes an ideal slate for quick responses.

Activities. The Activities for Teaching section is the heart of the lesson; it starts on the left page and continues to the right page. These are the instructions for teaching the lesson. The expected answers from the child are given in square brackets.

Establish with the children some indication when you want a quick response and when you want a more thoughtful response. Research shows that the quiet time for thoughtful response should be about three seconds. Avoid talking during this quiet time; resist the temptation to rephrase the question. This quiet time gives the slower child time to think and the quicker child time to think more deeply.

Encourage the child to develop persistence and perseverance. Avoid giving hints or explanations too quickly. Children tend to stop thinking once they hear the answer.

Explanations. Special background notes for the teacher are given in Explanations.

Worksheets. The worksheets are designed to give the children a chance to think about and to practice the day's lesson. The children are to do them independently. Some lessons, especially in the early levels, have no worksheet.

Games. Games, not worksheets or flash cards, provide practice. The games, found in the *Math Card Games* book, can be played as many times as necessary until proficiency or memorization takes place. They are as important to learning math as books are to reading. The *Math Card Games* book also includes extra games for the child needing more help, and some more challenging games for the advanced child.

In conclusion. Each lesson ends with a short summary called, "In conclusion," where the child answers a few short questions based on the day's learning.

Number of lessons. Generally, each lesson is be done in one day and each manual, in one school year. Complete each manual before going on to the next level. Other than Level A, the first lesson in each level is an introductory test with references to review lessons if needed.

Comments. We really want to hear how this program is working. Please let us know any improvements and suggestions that you may have.

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Table of Contents

Level B

Lesson 1*	Quantities 1 to 3
Lesson 2*	Quantities 1 to 5
Lesson 3*	Quantities 1 to 6 and the Abacus
Lesson 4*	Quantities 1 to 7, Taps, and Writing Numbers
Lesson 5*	Quantities 1 to 8
Lesson 6*	Quantities 9 and 10
Lesson 7*	
	Building the Stairs The Place-Value Cards and Translations
Lesson 8 (2 or 3 days) Lesson 9*	Part-Whole Circles
Lesson 10*	Solving Problems Partitioning Numbers 2 to 5
Lesson 11*	Partitioning Numbers 2 to 5
Lesson 12*	Mastering Partitioning 5
Lesson 13*	Nickels and Pennies
Lesson 14*	Simple Money Problems
Lesson 15	Partitioning 10
Lesson 16 (2 or 3 days)	Practicing the Tens Combinations
Lesson 17*	Quantities Arranged by Twos
Lesson 18*	Evens and Odds
Lesson 19*	More About Evens and Odds
Lesson 20*	Writing Addition Equations
Lesson 21	Writing More Equations & Parallel
Lesson 22*	Adding on the Abacus & Perpendicular
Lesson 23*	Introducing Tens
Lesson 24	Partitioning and Adding Tens
Lesson 25	Introducing Hundreds & Rectangle Design
Lesson 26	More Hundreds & Building Rectangles
Lesson 27	Rectangles from Tiles & the Commutative Property
Lesson 28	Thousands & Patterning
Lesson 29	Tens and Ones & Right Triangles
Lesson 30	Base-10 Picture Cards
Lesson 31	Overlapping the Place-Value Cards
Lesson 32	Large Numbers & Adding Tens and Ones
Lesson 33	More Right Triangles & Practice Sheets
Lesson 34	Trading with the Base-10 Pictures
Lesson 35	Adding with the Base-10 Pictures
Lesson 36	Derived Strategies & More Partitioning
Lesson 37	Dimes & Problems
Lesson 38 (2 or 3 days)	Test & the Tens Fractal
Lesson 39 (2 or 3 days)	More Adding with the Base-10 Pictures
Lesson 40	Quantities on Side 2 of the Abacus
Lesson 41 (2 days)	Tens' Traditional Names & Numbers in Order
Lesson 42	More About Tens
Lesson 43	Traditional Names for the Teens
LESSUII 43	Traditional maines for the Teens

 $[\]ensuremath{^*}$ A child who has completed all of Level A may skip these lessons.

Level B-page 2

Lesson 44 (1 to 3 days) Counting by 5s & Making Calendars

Working with Teens Lesson 45

Lesson 46 (1 or 2 days) Tens in 1000 & Sum of Numbers 1 to 10 Days in a Year and Dishes in the Cupboard Lesson 47

Lesson 48 (2 days) Math Balance & Bead Trading Lesson 49 Math Balance Equations

Lesson 50 Partitioning 15 & Adding 1 to a Number

Lesson 51 Adding 10 to a Number

Lesson 52 Adding 100 & Hours on a Clock Halves & Half Hours on a Clock Lesson 53 O'Clocks & Half Hours Practice Lesson 54 (1 or 2 days)

Five Minutes on the Clock Lesson 55

Lesson 56 (2 or 3 days) Minute Practice

Lesson 57 Adding Dimes, Nickels, and Pennies

Lesson 58 Choosing Coins

Lesson 59 (2 days) Test & Corners Exercise

Corners Game Lesson 60 (2 days)

Lesson 61 Combinations with 9 by Completing the 10 Lesson 62 Introducing Geoboards & 9s Combinations

Lesson 63 Sums Equal to 11 Lesson 64 Congruent Rectangles Lesson 65 Designs with Diagonals

The Two-Fives Strategy & Patterning Lesson 66

Two-Fives Strategy Practice & Mirror Symmetry Lesson 67 Lesson 68 Tile Symmetry & 2-Fives in Higher Decades

Lesson 69 Combinations with 8s

Lesson 70 Geoboard Patterning & Combinations with 8s

Lesson 71 Adding 2-Digit Numbers & Symmetry Lesson 72 Flipping Vertically and Horizontally Lesson 73

Two-Digit Numbers Plus a Multiple of Ten

Lesson 74 Finding the Number of Cubes

Lesson 75 Adding 2-Digit Numbers With Sums Over 100

Lesson 76 Mentally Adding 2-Digit Numbers Lesson 77 Partitioning Numbers into Three Parts Adding More Than Two Addends Lesson 78

Lesson 79 Numbers Totaling 15 & Rows and Columns Lesson 80 More on Mentally Adding 2-Digit Numbers

Lesson 81 Even and Odd Numbers up to 100

Lesson 82 **Even-Odd Adding Rules** Lesson 83 Continuing the Pattern

Lesson 84 Continuing Patterns Up and Down

Lesson 85 Skip Counting

Lesson 86 Quarters

Lesson 87 Quarter of a Dollar Lesson 88 Patterns in the Hundreds Lesson 89 Reviewing Place Value

Level B-page 3

Lesson 90 (5 days) Adding Four-Digit Numbers on the Abacus Lesson 91 (several days) Adding Four-Digit Numbers on Paper

Lesson 92 The > and < Symbols
Lesson 93 Introducing Subtraction

Lesson 94 Subtraction as the Missing Addend

Lesson 95 Making Change

Lesson 96 More Making Change Activities Lesson 97 Introduction to Measuring

Lesson 98 (2 days) Finding Perimeter

Lesson 99 (2 days) Finding Rectangles with a Given Perimeter & Diagonals

Lesson 100 Measuring Long Distances & Estimating
Lesson 101 Constructing Triangles & Finding Perimeters

Lesson 102 (2 days) Subtracting by Going Back

Lesson 103 Reading Scales
Lesson 104 Time to the Minute
Lesson 105 Halves and Fourths

Lesson 106 (1 or 2 days) Graphing Lesson 107 Final Test

Practice Record & Practice Sheets

Tests Appendix

Lesson 48 (2 days)

Math Balance & Bead Trading

OBJECTIVES

- 1. To introduce the math balance
- 2. To learn the terms balanced and level
- 3. To practice trading on side 2 of the abacus

MATERIALS Math balance

Abacus

20 to 30 basic number cards 1 to 9

WARM-UP

Ask the child to count by tens to 300.

Ask the child to count aloud by 5s to 100 by entering 5s on the abacus.

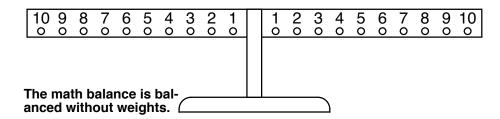
Enter various teen numbers on the abacus and ask the child to name them without counting.

For mental computation ask, $\underline{\text{How much is } 40 + 2?}$ [42] $\underline{\text{How much}}$ is 40 + 6? [46] $\underline{\text{How much is } 40 + 10?}$ [50]

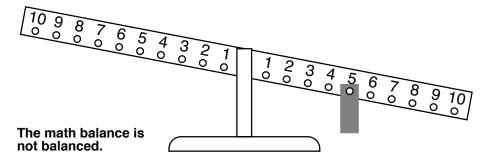
ACTIVITIES

Math balance. Show the child the math balance. Explain that the beam is *balanced*, or *level*, as it is without any weights, when it is parallel to the table or floor. See the figure below.

Note: Adjust the small weights at the back center of the balance to ensure that it is level without weights.

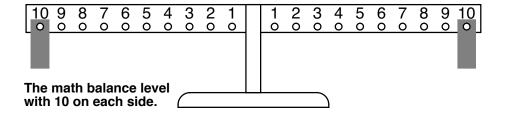


Enter a weight at the 5-peg on the right side as shown below and ask, <u>Is it balanced?</u> [no]

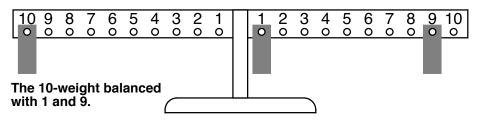


Balancing with two weights. Give the child 2 weights and ask him, Enter the weights so it will balance. [Most likely he will choose the two 10s.] See the figure on on the next page. Ask him if there are any other places where they will balance. [1 & 1, 2 & 2, and so forth] Ask him to write down what he has found that balances. Use the letter *b* to mean balance. For example,

10 b (balances) 10



Balancing with 3 weights. Remove the weight at the right 10-peg and ask the child to use 2 weights on the right side to balance it. See the figure below. [1 & 9 (shown), 2 & 8, 3 & 7, 4 & 6, or 5 & 5] Ask him to find the other ways. Record the results as follows:



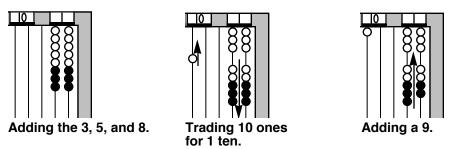
10 b (balances) 1 + 9

Ask the child to find more ways to balance it with 3 weights and to write down his results. The single weight can be on either side.

Bead Trading game. Show the child how to play this individual trading game. Take a stack of number cards. The cards are placed face down on a stack within reach of the player.

The object of the game is to add the quantities as indicated on the cards. A player turns over the top card and enters that many beads in the ones columns. Without regard to turn, each player takes the top card from the stack.

Play a sample game on the abacus. Arrange the cards so the top cards are 3, 5, 8, and 9. Enter the 3 and 5 on side 2 in the ones column. Ask the child if he could trade. [no] Add the 8 and again ask if he could trade. [yes] Trade. Then add 9. See the figures below.



Continue with more numbers until the child understands. Ask what he will do when he has 10 tens. [Trade for 1 hundred.]

Cards are reused as needed. Tell the child that when the reaches 100, he is a *champion*. When he reaches 1000, he is a *grand champion*.

Many children enjoy continuing the game from day to day. He can record his final numbers and continue from there the next time.

Note: If the child discover that the "b" in the written work can be replaced by the equal sign, tell them to use it in place of the "b"

Lesson 76

Mentally Adding 2-Digit Numbers

OBJECTIVE 1. To mentally add 2-digit numbers

MATERIALS Hundred chart, optional

Worksheet 29, Mentally Adding 2-Digit Numbers

WARM-UP Ask the child to give the ways to make 10, 1 and what? [9] 4 and what? [6] 7 and what? [3] 2 and what? [8]

Ask the child the following: 6 + 7 [13], 9 + 3 [12], 8 + 5 [13], 7 + 9 [16], and 3 + 4. [7]

Ask the child to give the sums for 32 + 60 [92], 92 + 6 [98], 58 + 20 [78], 78 + 8 [86] and 46 + 40. [86]

NOTE

Studies show that in the course of everyday life, most people needing to add two 2-digit numbers do so in their heads. They do not reach for paper and pencil, nor do they use a calculator. This lesson gives the child a systematic method, or algorithm, for accomplishing mental adding. The next lesson will focus on shortcuts.

ACTIVITIES

Adding 2-digit numbers. Give the child the following or similar problem. There are 24 boys and 20 girls playing in the park. Then 3 more girls come out to play. How many children are playing now in the park? [47] Read the problem several times.

After the child arrives at the answer, ask him to write the equation on the drawing board. [24 + 20 + 3 = 47] Research shows that, generally, writing equations does not help young children solve problems. Hence, it is suggested he write the equation after solving the problem.

Ask the child how he did the adding. The numbers in the problem were given in the most efficient order for adding 2-digit numbers. Discuss whether he thinks it is a good way to add the numbers.

Practice. Write and say,

$$35 + 23 =$$

Ask the child if he could add these numbers by starting with 35, then adding the tens, 20, and then 3. Model it for the child by saying, 35 + 20 = 55 and 55 + 3 = 58.

Ask the child to practice with 47 + 32. [77, 79] Encourage him to say the intermediate sum. Repeat for 26 + 44. [66, 70]

Continue by asking if he is ready for some harder numbers. Give him the following examples, which require trading with the ones.

$$36 + 36 = [66, 72]$$

 $69 + 28 = [89, 97]$

Ask him also to try some still harder ones. These have trading in the tens.

$$56 + 56 = [106, 112]$$

 $86 + 39 = [116, 125]$

EXTRA HELP Using a hundred square may help the child. For example, to add 35 + 23, first locate the 35. Next to add 20, move down two columns to 55; lastly, to add 3, move to the right three spaces. If the hundred chart is used, be certain that the child understands why it works.

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35)	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55)	56	57	58	59	60
51 61					56 66				60 70
-	62	63	64	65		67	68	69	
61	62	63	64 74	65 75	66	67 77	68 78	69	70

Adding 35 + 23 on a hundred chart by using the tens and the ones.

Worksheet. Worksheet 29 gives the child practice in adding mentally, that is, without the abacus, although, you might want to ask him to check his work with it. The examples and problems are shown below.

	21 + 15 = 36
	15 + 17 = 32
	54 + 57 = 111
	19 + 19 = 38
	24 + 43 = 67
	37 + 26 = 63
	64 + 56 = 120
	67 + 29 = 96
53 + 45 = 98	95 + 59 = 154
36 + 56 = 92	27 + 67 = 94
58 + 59 = 117	16 + 18 = 34
85 + 44 = 129	28 + 37 = 65

Practice sheets. The child should continue using the practice sheets until the facts are mastered.

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To see the pattern, find your answers and mark the squares when your answer is less than 100.

Name_

10	20	30	40	9	09	02	80	06	100
6	19	29	68	49	69	69	62	68	66
8	18	28	38	48	28	89	82	88	86
2	11	22	28	47	29	2 9	<i>22</i>	28	26
9	16	26	36	46	99	99	92	98	96
2	15	25	32	45	22	<u> </u>	<u> </u>	85	92
4	14	24	34	44	54	64	74	84	94
8	13	23	88	43	23	£9	23	83	93
2	12	22	32	42	52	62	72	82	92
1	11	21	31	41	51	61	71	81	91

23+42=	=99+98	58+59 =	= + + + 5 8

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2	_	^	6	m	9	9	6	6	^	8	<u></u>
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+	+	+	+	+	+	+	+	+	+	+	+
	2	 	6	士	^	 	1	95	^	9	8
7	—	വ		7	m	9	9	6	~		N
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